

*Generalized Roll 02.sas:*

*Simulated generalized Roll model (Ch. 8)*

*10000 observations with  $c=1$ ,  $\lambda=2$ , and std.dev. of  $u = 1$*

*Start of (simulated) sample*

m	t	q	u	p
3.1310	1	1	1.13105	4.1310
7.1400	2	1	2.00893	8.1400
6.6896	3	1	- 2.45036	7.6896
8.6692	4	1	- 0.02043	9.6692
5.1788	5	- 1	- 1.49036	4.1788
1.6576	6	- 1	- 1.52125	0.6576
- 3.7683	7	- 1	- 3.42593	- 4.7683
- 1.3694	8	1	0.39892	- 0.3694
- 3.2336	9	- 1	0.13581	- 4.2336
- 2.2175	10	1	- 0.98391	- 1.2175
- 0.6989	11	1	- 0.48139	0.3011
0.5021	12	1	- 0.79894	1.5021
- 2.3574	13	- 1	- 0.85954	- 3.3574
- 4.3484	14	- 1	0.00900	- 5.3484
- 5.6531	15	- 1	0.69528	- 6.6531
- 8.4250	16	- 1	- 0.77188	- 9.4250
- 10.6604	17	- 1	- 0.23541	- 11.6604
- 8.7257	18	1	- 0.06533	- 7.7257
- 9.5504	19	- 1	1.17532	- 10.5504
- 12.1547	20	- 1	- 0.60428	- 13.1547

# Univariate MA analysis of $p$ Input dataset=pq maOrder=1

## The ARIMA Procedure

Name of Variable = p	
Period(s) of Differencing	1
Mean of Working Series	0
Standard Deviation	3.310097
Number of Observations	9999
Observation(s) eliminated by differencing	1

Autocorrelations				
Lag	Covariance	Correlation	-1 9 8 7 6 5 4 3 2 1 0 1 2 3 4 5 6 7 8 9 1	Std Error
0	10.956740	1.00000	*****	0
1	- 2.860552	- .26108	*****	0.010001
2	- 0.108014	- .00986		0.010660
3	- 0.027610	- .00252		0.010661
4	0.061780	0.00564		0.010661
5	0.151746	0.01385		0.010662
6	- 0.247448	- .02258		0.010663
7	0.046133	0.00421		0.010668
8	0.122235	0.01116		0.010668
9	0.043863	0.00400		0.010670
10	- 0.104152	- .00951		0.010670

". " marks two standard errors

Inverse Autocorrelations	
Lag	Correlation
1	0.28780   *****
2	0.09127   **
3	0.02694   *
4	0.00003
5	- 0.00581
6	0.01347
7	- 0.00251
8	- 0.01328
9	- 0.00677
10	0.00449

## Univariate MA analysis of $p$ Input dataset=pq maOrder=1

### The ARIMA Procedure

Partial Autocorrelations																						
Lag	Correlation	-1	9	8	7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	1
1	- 0.26108	*****																				
2	- 0.08373	**																				
3	- 0.02936	*																				
4	- 0.00395																					
5	0.01503																					
6	- 0.01543																					
7	- 0.00510																					
8	0.00998																					
9	0.01018																					
10	- 0.00489																					

Autocorrelation Check for White Noise									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	690.13	6	<.0001	-0.261	-0.010	-0.003	0.006	0.014	-0.023

Conditional Least Squares Estimation					
Parameter	Estimate	Standard Error	t Value	Approx Pr >  t	Lag
MA1,1	0.28834	0.0095735	30.12	<.0001	1

Variance Estimate	10.13235
Std Error Estimate	3.183135
AIC	51531.95
SBC	51539.16
Number of Residuals	9999

\* AIC and SBC do not include log determinant.

# Univariate MA analysis of $p$ Input dataset= $pq$ maOrder=1

## The ARIMA Procedure

Autocorrelation Check of Residuals									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	6.52	5	0.2587	0.003	- 0.010	- 0.003	0.008	0.011	- 0.019
12	10.07	11	0.5239	0.003	0.013	0.006	- 0.007	0.004	- 0.008
18	17.85	17	0.3987	- 0.007	0.012	- 0.023	- 0.001	0.003	- 0.006
24	23.00	23	0.4610	0.014	0.009	- 0.003	- 0.015	0.002	- 0.000
30	24.98	29	0.6794	- 0.004	- 0.010	- 0.001	0.001	0.009	- 0.001
36	26.28	35	0.8560	0.006	0.004	- 0.004	- 0.005	- 0.003	- 0.005
42	33.58	41	0.7879	0.011	0.004	- 0.020	0.013	- 0.004	- 0.003
48	38.81	47	0.7965	- 0.008	- 0.006	- 0.008	- 0.017	0.007	- 0.003

Model for variable p	
Data have been centered by subtracting the value	- 0.02005
Period(s) of Differencing	1

No mean term in this model.

Moving Average Factors	
Factor 1:	1 - 0.28834 B**(1)

## *Univariate random- walk analysis*

Innovation variance
10.132349

Thetas
1
- 0.288342

Sum of thetas, including theta(0)=1
0.71166

Random- walk variance
5.13159748390164

Random- walk standard deviation
2.26530295631768

Pricing error coefficients
- 0.28834

Pricing error variance (lower bound)
0.8424158508

Pricing error standard deviation (lower bound)
0.917832

*Generalized Roll 02.sas:*

*Simulated generalized Roll model (Ch. 8)*

*10000 observations with  $c=1$ ,  $\lambda=2$ , and std.dev. of  $u = 0$*

*(Special case of no public information)*

*Start of (simulated) sample*

m	t	q	u	p
2	1	1	0	3
4	2	1	0	5
6	3	1	0	7
8	4	1	0	9
6	5	-1	0	5
4	6	-1	0	3
2	7	-1	0	1
4	8	1	0	5
2	9	-1	0	1
4	10	1	0	5
6	11	1	0	7
8	12	1	0	9
6	13	-1	0	5
4	14	-1	0	3
2	15	-1	0	1
0	16	-1	0	-1
-2	17	-1	0	-3
0	18	1	0	1
-2	19	-1	0	-3
-4	20	-1	0	-5

# Univariate MA analysis of $p$ Input dataset=pq maOrder=1

## The ARIMA Procedure

Name of Variable = p	
Period(s) of Differencing	1
Mean of Working Series	0
Standard Deviation	3.155479
Number of Observations	9999
Observation(s) eliminated by differencing	1

Autocorrelations				
Lag	Covariance	Correlation	-1 9 8 7 6 5 4 3 2 1 0 1 2 3 4 5 6 7 8 9 1	Std Error
0	9.957050	1.00000	*****	0
1	- 2.912645	- .29252	*****	0.010001
2	- 0.071172	- .00715		0.010822
3	- 0.030768	- .00309		0.010823
4	0.062856	0.00631		0.010823
5	0.072457	0.00728		0.010823
6	- 0.241978	- .02430		0.010824
7	0.074450	0.00748		0.010829
8	0.040461	0.00406		0.010830
9	0.0020427	0.00021		0.010830
10	- 0.086366	- .00867		0.010830

". " marks two standard errors

Inverse Autocorrelations		
Lag	Correlation	-1 9 8 7 6 5 4 3 2 1 0 1 2 3 4 5 6 7 8 9 1
1	0.32874	*****
2	0.11497	**
3	0.04012	*
4	0.01003	
5	0.00755	
6	0.02202	
7	0.00466	
8	- 0.00096	
9	0.00267	
10	0.00713	

# Univariate MA analysis of $p$ Input dataset=pq maOrder=1

## The ARIMA Procedure

Partial Autocorrelations																						
Lag	Correlation	-1	9	8	7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	1
1	-0.29252	*****																				
2	-0.10139	**																				
3	-0.03873	*																				
4	-0.00757																					
5	0.00717																					
6	-0.02133																					
7	-0.00622																					
8	0.00231																					
9	0.00222																					
10	-0.00800																					

Autocorrelation Check for White Noise									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	863.30	6	<.0001	-0.293	-0.007	-0.003	0.006	0.007	-0.024

Conditional Least Squares Estimation					
Parameter	Estimate	Standard Error	t Value	Approx Pr >  t	Lag
MA1,1	0.32912	0.0094426	34.85	<.0001	1

Variance Estimate	8.999207
Std Error Estimate	2.999868
AIC	50346.1
SBC	50353.31
Number of Residuals	9999

\* AIC and SBC do not include log determinant.



# Univariate MA analysis of $p$ Input dataset= $pq$ maOrder=1

## The ARIMA Procedure

Autocorrelation Check of Residuals									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	6.47	5	0.2631	0.003	- 0.007	- 0.004	0.006	0.002	- 0.023
12	8.70	11	0.6499	0.002	0.005	- 0.000	- 0.006	0.008	- 0.009
18	14.50	17	0.6317	- 0.011	0.009	- 0.018	0.003	0.004	- 0.005
24	20.93	23	0.5852	0.012	0.009	- 0.002	- 0.019	0.007	0.003
30	23.41	29	0.7574	0.005	- 0.004	- 0.000	- 0.010	0.008	- 0.007
36	25.35	35	0.8848	0.001	- 0.008	- 0.004	0.001	- 0.006	- 0.008
42	35.77	41	0.7019	0.009	- 0.005	- 0.027	0.014	- 0.006	- 0.002
48	38.89	47	0.7939	- 0.010	- 0.009	- 0.004	- 0.007	- 0.003	- 0.007

Model for variable $p$	
Data have been centered by subtracting the value	- 0.0186
Period(s) of Differencing	1

No mean term in this model.

Moving Average Factors	
Factor 1:	1 - 0.32912 B**(1)

## *Univariate random- walk analysis*

Innovation variance
8.9992071

Thetas
1
- 0.329118

Sum of thetas, including theta(0)=1
0.67088

Random- walk variance
4.0503838277044

Random- walk standard deviation
2.01255654025033

Pricing error coefficients
- 0.32912

Pricing error variance (lower bound)
0.9747836273

Pricing error standard deviation (lower bound)
0.987311

*Generalized Roll 02.sas:*

*Simulated generalized Roll model (Ch. 8)*

*10000 observations with  $c=1$ ,  $\lambda=0$ , and std.dev. of  $u = 1$*

*(Special case of no private information)*

*Start of (simulated) sample*

m	t	q	u	p
1.13105	1	1	1.13105	2.13105
3.13998	2	1	2.00893	4.13998
0.68962	3	1	-2.45036	1.68962
0.66920	4	1	-0.02043	1.66920
-0.82116	5	-1	-1.49036	-1.82116
-2.34241	6	-1	-1.52125	-3.34241
-5.76834	7	-1	-3.42593	-6.76834
-5.36942	8	1	0.39892	-4.36942
-5.23361	9	-1	0.13581	-6.23361
-6.21752	10	1	-0.98391	-5.21752
-6.69891	11	1	-0.48139	-5.69891
-7.49785	12	1	-0.79894	-6.49785
-8.35739	13	-1	-0.85954	-9.35739
-8.34839	14	-1	0.00900	-9.34839
-7.65311	15	-1	0.69528	-8.65311
-8.42499	16	-1	-0.77188	-9.42499
-8.66039	17	-1	-0.23541	-9.66039
-8.72572	18	1	-0.06533	-7.72572
-7.55040	19	-1	1.17532	-8.55040
-8.15468	20	-1	-0.60428	-9.15468

# Univariate MA analysis of $p$ Input dataset=pq maOrder=1

## The ARIMA Procedure

Name of Variable = p	
Period(s) of Differencing	1
Mean of Working Series	0
Standard Deviation	1.723524
Number of Observations	9999
Observation(s) eliminated by differencing	1

Autocorrelations				
Lag	Covariance	Correlation	-1 9 8 7 6 5 4 3 2 1 0 1 2 3 4 5 6 7 8 9 1	Std Error
0	2.970536	1.00000	*****	0
1	- 0.955313	- .32160	*****	0.010001
2	- 0.029518	- .00994		0.010986
3	- 0.0069166	- .00233		0.010987
4	- 0.0053635	- .00181		0.010987
5	0.057462	0.01934		0.010987
6	- 0.063592	- .02141		0.010991
7	0.0059357	0.00200		0.010995
8	0.031327	0.01055		0.010995
9	0.022782	0.00767		0.010996
10	- 0.032818	- .01105		0.010996

". " marks two standard errors

Inverse Autocorrelations		
Lag	Correlation	-1 9 8 7 6 5 4 3 2 1 0 1 2 3 4 5 6 7 8 9 1
1	0.37387	*****
2	0.14929	***
3	0.05911	*
4	0.01883	
5	- 0.00147	
6	0.01067	
7	- 0.00273	
8	- 0.01499	
9	- 0.01141	
10	0.00212	

# Univariate MA analysis of $p$ Input dataset=pq maOrder=1

## The ARIMA Procedure

Partial Autocorrelations																						
Lag	Correlation	-1	9	8	7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	1
1	- 0.32160	*****																				
2	- 0.12644	***																				
3	- 0.05281	*																				
4	- 0.02398																					
5	0.01138																					
6	- 0.01274																					
7	- 0.00823																					
8	0.00734																					
9	0.01510																					
10	- 0.00247																					

Autocorrelation Check for White Noise									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	1043.85	6	<.0001	-0.322	-0.010	-0.002	-0.002	0.019	-0.021

Conditional Least Squares Estimation					
Parameter	Estimate	Standard Error	t Value	Approx Pr >  t	Lag
MA1,1	0.37440	0.0092725	40.38	<.0001	1

Variance Estimate	2.613018
Std Error Estimate	1.616483
AIC	37981.03
SBC	37988.24
Number of Residuals	9999

\* AIC and SBC do not include log determinant.

# Univariate MA analysis of p Input dataset=pq maOrder=1

## The ARIMA Procedure

Autocorrelation Check of Residuals									
To Lag	Chi- Square	DF	Pr > ChiSq	Autocorrelations					
6	6.21	5	0.2867	0.004	- 0.010	- 0.005	0.001	0.014	- 0.016
12	10.21	11	0.5114	0.001	0.014	0.010	- 0.007	0.002	- 0.007
18	18.66	17	0.3481	0.000	0.019	- 0.018	0.001	0.000	- 0.012
24	22.83	23	0.4707	0.006	0.006	- 0.003	- 0.013	0.005	0.012
30	28.11	29	0.5119	- 0.002	- 0.009	0.000	0.010	0.015	0.011
36	31.26	35	0.6495	0.008	0.005	- 0.008	- 0.012	0.002	0.001
42	38.24	41	0.5938	0.013	0.008	- 0.020	0.006	- 0.003	0.004
48	46.95	47	0.4744	0.005	- 0.001	- 0.006	- 0.014	0.024	- 0.000

Model for variable p	
Data have been centered by subtracting the value	- 0.00145
Period(s) of Differencing	1

No mean term in this model.

Moving Average Factors	
Factor 1:	1 - 0.3744 B**(1)

## *Univariate random- walk analysis*

Innovation variance
2.6130179

Thetas
1
- 0.374397

Sum of thetas, including theta(0)=1
0.62560

Random- walk variance
1.02268060796994

Random- walk standard deviation
1.01127672175816

Pricing error coefficients
- 0.37440

Pricing error variance (lower bound)
0.3662748799

Pricing error standard deviation (lower bound)
0.605206